



Early Journal Content on JSTOR, Free to Anyone in the World

This article is one of nearly 500,000 scholarly works digitized and made freely available to everyone in the world by JSTOR.

Known as the Early Journal Content, this set of works include research articles, news, letters, and other writings published in more than 200 of the oldest leading academic journals. The works date from the mid-seventeenth to the early twentieth centuries.

We encourage people to read and share the Early Journal Content openly and to tell others that this resource exists. People may post this content online or redistribute in any way for non-commercial purposes.

Read more about Early Journal Content at <http://about.jstor.org/participate-jstor/individuals/early-journal-content>.

JSTOR is a digital library of academic journals, books, and primary source objects. JSTOR helps people discover, use, and build upon a wide range of content through a powerful research and teaching platform, and preserves this content for future generations. JSTOR is part of ITHAKA, a not-for-profit organization that also includes Ithaka S+R and Portico. For more information about JSTOR, please contact support@jstor.org.

Solution by BENJ. F. YANNEY, A. M., Professor of Mathematics, Mount Union College, Alliance, O.

In THE AMERICAN MATHEMATICAL MONTHLY, No. 1, Vol. I, Dr. Dickson gives the following formulæ for finding lowest integers representing the sides of a right triangle: $m + \sqrt[4]{(2mn)}$, $n + \sqrt[4]{(2mn)}$, $m + n + \sqrt[4]{(2mn)}$, in which m and n are shown to be integers, prime to each other, the one an odd square, the other twice any square, except such as would make m and n have a common factor.

We may represent, then, m and n by $(2r+1)^2$ and $2s^2$, respectively.

Now, if any one of the three sides of a rational right triangle is divisible by 5, so then also is their product; and, conversely.

The product of the three sides, represented by the above formulae, is $5m^2n + 5mn^2 + 5mn\sqrt[4]{(2mn)} + (m^2 + n^2)\sqrt[4]{(2mn)}$, the first three terms of which are evidently divisible by 5. Then, substituting in the last term for m and n their equals, $(2r+1)^2$ and $2s^2$, we have

$$2s(2r+1)[(2r+1)^4 + 4s^4] \dots (1).$$

Again, all possible integers may be represented by $5k+1$, $5k+2$, $5k+3$, $5k+4$, and $5k+5$.

It is plain that if $s=5k+5$, (1) will be divisible by 5, no matter what value r may have. So, too, if $r=5k+2$, no matter what s may equal. We still have to show that the last factor of (1) is divisible by 5 when s has any other value than $5k+5$, while at the same time r has any other value than $5k+2$.

Note that under these conditions all the literal terms of $(2r+1)^4$ and $4s^4$ are divisible by (5), while the numerical term of $(2r+1)^4$ always ends with 1, and that of $4s^4$ with 4; hence the numerical term of $(2r+1)^4 + 4s^4$ always ends with 5. Therefore, in any case, (1) is divisible by 5, which proves the proposition.

COROLLARY. By the same method, it may be proven that one of the numbers representing the legs of a rational right triangle must be divisible by 3. Dr. Dickson has shown that one must be divisible also by 4.

PROBLEMS FOR SOLUTION.

ARITHMETIC.

134. Proposed by ALOIS F. KOVARIK, Instructor in Mathematics and Science, Decorah Institute, Decorah, Iowa.

A certain piece of land is surrounded by a four-board fence, the boards being 16 feet long. The number of acres in the land equals the number of boards in the fence. How many acres in the land?

135. Proposed by NELSON L. RORAY, Brigdeton, N. J.

If 6 is one-half of 10, what part of 20 is 12? Also what part of 30 is 10?

*** Solutions of these problems should be sent to B. F. Finkel not later than Dec. 10.